

Projectile Motion

$$x = x_0 + (v_0 \cos \alpha) t \quad y = y_0 + (v_0 \sin \alpha) t - \frac{1}{2} g t^2$$

Vector Functions

$$\mathbf{T}(t) = \frac{\mathbf{r}'(t)}{\|\mathbf{r}'(t)\|} \quad \mathbf{N}(t) = \frac{\mathbf{T}'(t)}{\|\mathbf{T}'(t)\|} \quad a_T = \mathbf{a} \cdot \mathbf{T} = \frac{d^2 s}{dt^2} = \frac{\mathbf{a} \cdot \mathbf{v}}{\|\mathbf{v}\|} \quad a_N = \mathbf{a} \cdot \mathbf{N} = \kappa \left(\frac{ds}{dt} \right)^2 = \frac{\|\mathbf{a} \times \mathbf{v}\|}{\|\mathbf{v}\|}$$

Curvature

$$\kappa = \frac{|y''|}{[1 + (y')^2]^{3/2}} \quad \text{or} \quad \frac{|x'y'' - x''y'|}{[(x')^2 + (y')^2]^{3/2}} \quad \text{or} \quad \frac{\|\mathbf{T}'(t)\|}{\|\mathbf{r}'(t)\|} \quad \text{or} \quad \frac{\|\mathbf{r}'(t) \times \mathbf{r}''(t)\|}{\|\mathbf{r}'(t)\|^3} \quad \text{or} \quad \frac{|\mathbf{a}(t) \cdot \mathbf{N}(t)|}{\|\mathbf{v}(t)\|^2}$$

Polar Coordinates

$$\begin{aligned} x &= r \cos \theta & r &= \sqrt{x^2 + y^2} \\ y &= r \sin \theta & \tan \theta &= \frac{y}{x} \end{aligned} \quad dA = r \, dr \, d\theta$$

Spherical Coordinates

$$\begin{aligned} x &= \rho \sin \phi \cos \theta & \rho &= \sqrt{x^2 + y^2 + z^2} \\ y &= \rho \sin \phi \sin \theta & \cos \phi &= \frac{z}{\sqrt{x^2 + y^2 + z^2}} \\ z &= \rho \cos \phi & \tan \theta &= \frac{y}{x} \end{aligned} \quad dV = \rho^2 \sin \phi \, d\rho \, d\phi \, d\theta$$

Vector Fields

$$\text{curl } \mathbf{F} = \nabla \times \mathbf{F} \quad \text{div } \mathbf{F} = \nabla \cdot \mathbf{F}$$

Green's Theorem

$$\int_C \mathbf{F} \cdot d\mathbf{r} = \iint_R \left(\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dA$$

Divergence Theorem

$$\iint_S \mathbf{F} \cdot \mathbf{N} \, dS = \iiint_Q \text{div}(\mathbf{F}) \, dV$$

Stokes' Theorem

$$\int_C \mathbf{F} \cdot d\mathbf{r} = \iint_S \text{curl}(\mathbf{F}) \cdot \mathbf{N} \, dS$$